Magnetic Bubble Chambers and Sub-GeV Dark Matter Direct Detection

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Abstract

We propose a new application of single molecule magnet crystals: their use as “magnetic bubble
chambers” for the direct detection of sub-GeV dark matter. The spins in these macroscopic crystals
effectively act as independent nano-scale magnets. When anti-aligned with an external magnetic
field they form meta-stable states with a relaxation time that can be very long at sufficiently low
temperatures. The Zeeman energy stored in this system can be released through localized heating,
caused for example by the scattering or absorption of dark matter, resulting in a spin avalanche (or
“magnetic deflagration”) that amplifies the effects of the initial heat deposit, enabling detection.
Much like the temperature and pressure in a conventional bubble chamber, the temperature and
external magnetic field set the detection threshold for a single molecule magnet crystal. We discuss
this detector concept for dark matter detection and propose ways to ameliorate backgrounds. If
successfully developed, this detector concept can search for hidden photon dark matter in the meV
- eV mass range with sensitivities exceeding current bounds by several orders of magnitude.
I. INTRODUCTION

The continuing null results from experiments aiming to directly detect dark matter (DM) with a mass above the GeV scale has stimulated theoretical and experimental excursions away from the WIMP paradigm. There exist well established experimental methods (ADMX, ADMX-HF) \cite{1-3} to probe DM particles such as axions and hidden photons with mass between 1 GHz - 100 GHz \(10^{-6} \text{ eV} - 10^{-4} \text{ eV}\). New ideas employing nuclear magnetic resonance (CASP\textsc{e}r) \cite{4}, lumped element circuits (DM Radio) \cite{5-7}, and torsion balance/accelerometer \cite{8} (Eot-Wash) technologies have been proposed to search for ultra-light DM candidates in the mass range \(10^{-22} \text{ eV} - 10^{-6} \text{ eV}\).

While existing WIMP direct detection techniques have successfully lowered their thresholds to allow detection of DM with mass greater than 100 MeV \cite{9-12}, it is theoretically possible that the DM is only somewhat lighter than conventional WIMPs and could lie in the mass range \(10^{-3} \text{ eV} - 100 \text{ MeV}\), a region for which no detection principle is known. In such a mass region DM particles can deposit energies \(\sim 10^{-3} \text{ eV} - 10 \text{ eV}\) through absorption and inelastic scattering that are not large enough to be visible in conventional bolometric experiments. On the other hand, protocols to search for ultra-light DM that do not rely on the deposited energy leverage the coherence of the ultra-light DM signal to build a measurable phase in an experiment. The coherence of the DM signal is inversely proportional to its mass and at masses greater than \(\sim 10^{-3} \text{ eV}\) the coherence time is too small to employ phase accumulation techniques deployed to search for ultra-light DM. See Refs. \cite{13-19} and Refs. \cite{20-24} for recent proposals sensitive to DM energy depositions down to \(\sim eV\) and \(\sim 10^{-3} \text{ eV}\), respectively.

Achieving sensitivity to such small energy deposits suggests the use of systems where some intrinsic energy gain is possible. These systems, in general, require the storage of energy in a meta-stable state. The deposition of a small amount of energy can potentially lead to an avalanche in the system, where the initial energy deposit causes relaxation of the meta-stable state, releasing stored energy. This energy release can cause additional relaxation resulting in a runaway process that amplifies the initial deposited energy, enabling detection. A well known system of this kind is the bubble chamber \cite{25}, in which a liquid is maintained at a super-critical combination of temperature and pressure such that the energy deposited by an incident particle locally triggers the formation of a bubble. Because of the runaway reaction, the response of the detector is not proportional to the initial energy deposited.
Thus, while these systems generally do not allow the measurement of the initial energy, very low thresholds, otherwise inaccessible, can be attained. Due to the low expected event rates, for a successful DM application it is important that the detector is stable for long (> year) timescales. It is also necessary to be able to reject radioactive backgrounds in the energy range of interest.

In this paper we propose the use of a relatively newly discovered type of crystal —single molecule (or molecular) magnets (SMMs)— as a magnetic version of the bubble chamber that can be tuned to be sensitive to $\sim 10^{-3}$ eV - 10 eV energy deposits relevant for sub-GeV DM detection. This paper is organised as follows. In Sec. II we present a conceptual overview of the detector. Following this overview, in Sec. III we review some relevant properties of SMMs, including details of their chemistry and synthesis. Sec. IV outlines the proposed detector concept in greater detail. This includes the tuning of the parameters of such a ‘magnetic bubble chamber’, the preparation of the crystal, and potential experimental backgrounds. To estimate the reach of such a detector, in Sec. V we project sensitivity to a dark photon model, finding an improvement of several orders of magnitude over existing stellar limits in the range $\sim 10^{-3}$ eV - 10 eV. We conclude in Sec. VI. The present discussion is preliminary in nature and substantial work, both conceptual and experimental, will be required to better assess the feasibility.

II. OVERVIEW

SMMs are molecular crystals in which the molecules act as tiny, essentially non-interacting magnets [26,28]. Their study is currently a rapidly developing field of chemistry—many 100s of new SMMs have been created since their discovery in the 90s— and, importantly, SMMs are easily and cheaply synthesized. Some SMMs are known to be fluorescent, opening the possibility that scintillating versions may be engineered, further enhancing their potential as particle detectors.

The basic idea for using SMMs as magnetic bubble chambers is as follows (see also Fig. II). The crystal is prepared such that an order one fraction of the nano-magnets are anti-aligned with an external magnetic field, and so exist in a meta-stable state. This can be achieved simply by cooling the crystal and applying an external magnetic field; at low temperatures ($\sim 0.1$ K–$2$ K) the magnetic relaxation (spin flip to the ground state) time can be of order years. (A larger fraction of anti-aligned nano-magnets could potentially be achieved by
FIG. 1. DM detector concept based on magnetic deflagration in molecular nanomagnet crystals. A DM event that deposits energy in the form of heat ignites a spin-flip avalanche in the crystal which is detected by the change in magnetic flux through a pick-up loop.

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deflagration can be rapidly turned off, effectively quenching the cascade process, in analogy to recompression in a bubble chamber; b) the material can be prepared in small sized grains with sufficiently poor thermal coupling between them, such that deflagrations are limited to single grains. Which technique will prove more effective will have to be decided after more work on the material synthesis and detector implementation are carried out. For the purpose of this paper we will simply show that precision magnetometers \[3\] can observe the magnetic signal due to spin reversal in a $\sim 10^3 \mu m^3$ region in $\sim 10^{-7}$ s and that the magnetic field can be turned off on a similar time-scale. This provides a very substantial tolerance to dead-times due to background events.

III. SINGLE MOLECULE MAGNETS

An introduction to SMMs that includes a review of magnetic deflagration can be found in e.g. \[30\]. Here we provide details that are necessary for our purposes, and introduce three parameters which play a role in the tuning of the proposed device: the effective magnet spin, $J$, the energy barrier, $U$, and the time constant relative to the fastest possible relaxation, $\tau_0$.

A molecule in an SMM crystal typically consists of a magnetic core surrounded by a non-magnetic shell. The magnetic core may consist of multiple metal ions coupled through non-magnetic centers (e.g. oxygen dianions), or the core may be a single metal ion. This core has large effective spin $J$ which, in case of multiple metal ions, arises from strong (super)exchange interactions coupling the smaller spins of individual ions, or in the case of a single metal ion, arises from the coupling of spin and orbital angular momentum \[31, 32\]. The magnetic core is surrounded by a non-magnetic shell (typically organic ligands such as acetate) which acts to separate the magnetic cores from each other such that the exchange interactions between the core spins are anomalously weak. This architecture permits the possibility of magnetic deflagration—the negligible intermolecular magnetic interactions allows for the spins to release locally stored Zeeman energy. On the other hand, the non-magnetic shell provides the thermal contact necessary to transport the released heat from one molecule to the next, encouraging magnetic relaxation of neighboring molecules.

The effective spin $J$ contains $(2J+1) M_J$ states, where the value of $M_J$ denotes the projection of $J$ along a preferred axis. Interaction between the effective spin $J$ and the crystal field causes a splitting of these $M_J$ states such that an energy barrier, $U$, arises
between $M_J = \pm J$ and $M_J = 0$ (for integer $J$) or $1/2$ (for half-integer $J$), with $M_J = J - 1, J - 2...$ states at predictable energies in between. This manifold of $M_J$ states is typically depicted as a double-well potential (figure 2). In the absence of a magnetic field, the $M_J = -J$ and $M_J = +J$ states are degenerate. An applied magnetic field, $B$, stabilizes one side of the well and destabilizes the other. The difference in energy between $M_J = -J$ and $M_J = +J$ states (the Zeeman energy) is given by $2\mu_B g_J J B$, where $g_J$ is the Landé g-factor of the molecule. A molecule in the newly created metastable state is protected from instant decay if $kT \ll U$; when it does decay it releases a phonon equal to the Zeeman energy.

The relaxation time $\tau$ for spins to flip in thermal equilibrium is given by

$$\frac{1}{\tau} = \frac{A_1}{1 + A_2 B^2} + C B^2 T + D T^n + \frac{1}{\tau_0} \exp(-U/kT),$$

where the four terms describe relaxation by quantum tunneling, direct, Raman, and Orbach relaxation, respectively. The constants, $A_1$, $A_2$, $C$, $D$, and $\tau_0$ are unique to each SMM; $U$ is the energy barrier described previously; $B$ is the applied field. The four terms are listed in the order in which they are the dominant relaxation process going from low to high temperature. In the absence of an applied field, relaxation time at low temperature is determined by relaxation through a quantum tunneling mechanism. The tunneling relaxation mechanism involves direct interactions between states on either side of the double well potential and relaxation occurs without the release of a phonon. The strong field dependence removes tunneling as a viable relaxation pathway in even a modest field. The remaining processes are phonon dependent. The direct process emits a single phonon equal to the Zeeman energy as the molecule relaxes from $| + J \rangle$ to $| - J \rangle$. It is
FIG. 3. Typical behaviour of magnetic relaxation time as a function of temperature for an SMM. The temperature dependence that dominates at high and intermediate temperatures is indicated. The low temperature behaviour approaches the limiting quantum mechanical tunneling relaxation time, denoted $\tau_{QM}$.

typically only appreciable in SMMs with single metal centers in large applied fields. Raman and Orbach relaxation processes are both two-phonon processes, where the absorption and emission of phonons proceeds through either virtual (Raman) or real (Orbach) excited states. The power dependence of Raman relaxation has been described for a number of systems, and is generally large ($n = 5 - 9$) due to the increasing availability of phonons for relaxation at higher temperatures [38].

The relaxation time is a strong function of both temperature and the applied magnetic field. At low temperatures ($\sim 0.1$ K) and high magnetic fields ($\gtrsim 0.1$ T), the relaxation times are very long ($\sim$ months - years) while at higher temperatures ($\sim 30$ K) the relaxation time can be as short as $\sim \tau_0 \sim 10^{-10} - 10^{-14}$ s. This behavior implies that localized heating can lead to a rapid rise in spin relaxation, releasing stored Zeeman energy. The released energy further heats up the sample, resulting in additional spin relaxation, resulting in the avalanche that is triggered by a localized energy deposit (for example, by DM scattering or absorption).

The dominant relaxation mechanism depends both on the type of SMM and the temperature. Consider, for example, Mn$_{12}$-acetate, a SMM with a magnetic core of 12 manganese ions. The primary relaxation pathways for Mn$_{12}$-acetate are [33]: tunneling (ground state to ground state), thermally assisted tunneling (excitation partially up the double well and then tunneling from this excited state), or Orbach relaxation (moving from one state to
the next up the double well through successive absorptions of phonons). Relaxation at low temperature is only through tunneling and is therefore very slow (on the order of months). At higher temperatures Orbach relaxation dominates and its speed is only limited by the pre-exponential term $\tau_0$, which can be very short. Thus, a localized change in temperature can rapidly change the relaxation time, permitting an avalanche.

The majority of SMMs can be chemically categorized in the following way: SMMs with a single metal ion versus multiple metal ions, and those metal ions can be d-block metals (transition metals) or f-block metals (Lanthanides/Actinides). The parameters $J$, $U$ and $\tau_0$ broadly characterize the properties of a given SMM, and in the 100s of SMMs synthesized in the past two decades their values vary widely:

$$1 < J < 45,$$

$$\sim 1K < U < 1815K,$$

$$\sim 10^{-6} s < \tau_0 < \sim 10^{-14} s.$$

As we will see in section IV these quantities set the threshold energy necessary to trigger magnetic deflagration. Some properties of the better known molecules in these categories are given in Tab. I Our initial focus is on SMMs featuring multiple transition metals, and a brief description of several of these may illustrate the ease of access and tunability of these materials.

The Mn$_6$ family of SMMs is one of the best studied families of single-molecule magnets [42]. These molecules feature two trigonal [Mn$_3$O]$^{7+}$ cores each with $S = 2$ or $S = 6$ which couple to each other such that the spin of the Mn$_6$ SMM can range from $J = 4$ to $J = 12$. The general synthetic strategy is as follows: Mn(ClO$_4$)$_2$·6H$_2$O is dissolved in methanol (MeOH), ethanol (EtOH), or acetonitrile (MeCN). To this solution is added a molar equivalent of of salicylaldoxime (where salicylaldoxime is abbreviated H-sao, and modified versions of this ligand are Me-sao or Et-sao when methyl (Me) or ethyl (Et) groups replace a proton (H) in a particular position), a carboxylic acid (RCO$_2$H where R can be a variety of organic groups), and a base (e.g. sodium methoxide). From this approach one can make, for example, [Mn$_6$O$_2$(H-sao)$_6$(O$_2$CPh)$_2$(MeCN)$_2$(H$_2$O)$_2$] [12] or [Mn$_6$O$_2$(Et-sao)$_6$(O$_2$CPh(CH$_3$)$_2$)$_2$(EtOH)$_6$] [44]. While both contain very similar Mn$_6$ cores, the change in organic groups changes bond angles sufficiently such that the magnetic properties change substantially; the former molecule has $J = 4$, $\tau_0 = 1.7 \times 10^{-8}$ s, and $U = 34$ K while the latter has $J = 12$, $\tau_0 = 2 \times 10^{-10}$ s, and $U = 86$ K. See figure 4 for the molecular struc-
tature of these compounds. The materials are relatively inexpensive. By simply scaling up the known synthesis of \([\text{Mn}_6\text{O}_2(\text{Et-sao})_6(\text{O}_2\text{CPh}(\text{CH}_3)_2)_2(\text{EtOH})_6]\), a kilogram of material could be made for less than 3000 US dollars.

### IV. DETECTOR CONCEPT AND REQUIREMENTS

As outlined in section II, a viable detector for sub-GeV-mass DM particles has to achieve a sufficient sensitivity with negligible background. We can gain sensitivity to DM energy deposits in the region \(\sim 10^{-3} \text{ eV} - 10 \text{ eV}\) through requiring that this be the threshold for triggering a deflagration.

The magnitude and properties of the background produced by various types of radiation in the very low energy regime of interest here is mostly unknown. It can be generally argued (e.g. [49]) that the event density from a \(\sim \) flat Compton background in an energy region of very small extent, such as the one considered here, is exceedingly small. Of course, it

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**TABLE I.** Properties of SMMs from four different families.

<table>
<thead>
<tr>
<th>SMM</th>
<th>(J)</th>
<th>(\tau_0 [s])</th>
<th>(U [K])</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Mononuclear Transition Metal SMMs</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>([\text{K}(2.2.2\text{-crypt})][\text{Fe}(\text{SiMe}_3)_3]_2)</td>
<td>7/2</td>
<td>(4.5 \times 10^{-10})</td>
<td>354</td>
<td>[39]</td>
</tr>
<tr>
<td><strong>Multinuclear Transition Metal SMMs</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>([\text{Mn}<em>{12}\text{O}</em>{12}(\text{O}_2\text{CC}_3\text{H}_3)_2\text{H}_2\text{O}])</td>
<td>10</td>
<td>(2.1 \times 10^{-7})</td>
<td>61</td>
<td>[40]</td>
</tr>
<tr>
<td>([\text{Mn}<em>{12}\text{O}</em>{12}(\text{O}_2\text{CC}_6\text{H}_4\text{Me})_16(\text{H}_2\text{O})_4])</td>
<td>10</td>
<td>(2.0 \times 10^{-10})</td>
<td>38</td>
<td>[41]</td>
</tr>
<tr>
<td>([\text{Mn}<em>{12}\text{O}</em>{12}(\text{O}_2\text{CC}_6\text{H}_4\text{Me})_16(\text{H}_2\text{O})_4])</td>
<td>10</td>
<td>(7.7 \times 10^{-9})</td>
<td>64</td>
<td>[41]</td>
</tr>
<tr>
<td>([\text{Mn}_6\text{O}_2(\text{saao})_6(\text{O}_2\text{CPh})_2\text{MeCN}_2(\text{H}_2\text{O})]_2)</td>
<td>4</td>
<td>(6.6 \times 10^{-8})</td>
<td>24</td>
<td>[42]</td>
</tr>
<tr>
<td>([\text{Mn}_6\text{O}_2(\text{Et-saao})_6(\text{O}_2\text{C}(\text{CH}_3)_3)_2(\text{EtOH})_5])</td>
<td>6</td>
<td>(3.0 \times 10^{-8})</td>
<td>30</td>
<td>[43]</td>
</tr>
<tr>
<td>([\text{Mn}_6\text{O}_2(\text{Et-saao})_6(\text{O}_2\text{C}(\text{CH}_3)_3)_2(\text{EtOH})_6])</td>
<td>12</td>
<td>(2.0 \times 10^{-10})</td>
<td>86</td>
<td>[44]</td>
</tr>
<tr>
<td>([\text{Fe}_4(\text{CH}_3\text{C}(\text{CH}_2\text{O})_3)_2(\text{dpm})_6])</td>
<td>5</td>
<td>(2.1 \times 10^{-8})</td>
<td>17</td>
<td>[45]</td>
</tr>
<tr>
<td><strong>Mononuclear Lanthanide SMMs</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>([\text{Dy}(\text{O}^\text{Bu})_2(\text{C}_5\text{H}_5\text{N})_5][\text{BPh}_4])</td>
<td>15/2</td>
<td>(1.2 \times 10^{-12})</td>
<td>1815</td>
<td>[46]</td>
</tr>
<tr>
<td><strong>Multinuclear Lanthanide SMMs</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>([\text{K}(18\text{-crown-6})][[<a href="%5Ctext%7BTHF%7D">\text{Me}_3\text{Si}</a>\text{Dy}]_2(\mu-\eta^2:\eta^2-\text{N}_2)_2])</td>
<td>29/2</td>
<td>(8.0 \times 10^{-9})</td>
<td>178</td>
<td>[47]</td>
</tr>
<tr>
<td>([\text{K}(18\text{-crown-6})][[<a href="%5Ctext%7BTHF%7D">\text{Me}_3\text{Si}</a>\text{Tb}]_2(\mu-\eta^2:\eta^2-\text{N}_2)_2])</td>
<td>23/2</td>
<td>(8.2 \times 10^{-9})</td>
<td>327</td>
<td>[48]</td>
</tr>
</tbody>
</table>
is possible that minute energy depositions from processes other than Compton scattering may become important in the extremely low-energy regime of interest here. This issue is common to all possible concepts for detectors attacking an entirely unexplored energy region and only experimental tests with actual materials will reveal which background sources may be problematic and how to reduce them to a manageable level.

The detector proposed here integrates signals above a threshold and hence does not provide a proper energy measurement. From the point of view of background rejection, this limitation can be mitigated by nothing that in most cases it is expected that energy depositions larger than those of interest will leave a “trail” of deflagrations. This is particularly true if the detector is finely segmented in grains (case b) in section II, allowing a high-energy veto to be applied. The possibility of adding scintillation to the techniques used to veto higher-energy events has also been already mentioned.

It is also important that the system is otherwise stable, i.e. a negligible rate of deflagrations occur without an interaction in the detector. This is the equivalent of the “dark rate” in a photodetector. While, given the large spin density, there will always be some non-negligible probability for a single spin to flip in a SMM crystal, parameters can be chosen...
so that a single spin flip cannot set off an avalanche, viz. the size of the initial hot region (i.e. our thresholds) needs to be at least a few spins (few angstroms) “long”. In this way, the probability for all these spins to simultaneously flip is very low and the dark rate can be arbitrarily reduced. On the other hand, the DM scattering deposits more energy than the Zeeman energy released by a single spin flip, raising the temperature of a larger region, triggering a deflagration.

We now conceptually discuss, in turn, the detector preparation, threshold tuning, deflagration quenching and reset.

A. Detector preparation

Preparation for an operating run consists of cooling the system to temperatures $\sim 0.1$ K, and then applying a magnetic field ($\sim 0.1 - 1$ T) to the sample. After this procedure, half of the spins will exist in the meta-stable well of the potential, as a result of the very long magnetic relaxation time at low temperature.

We require there to be no significant loss of usable detector after the preparation stage (i.e. that roughly half the spins end up in the meta-stable state—in particular that no avalanche occurs). Magnetic relaxation times under an applied magnetic field are typically longer than in the zero field case. This is due to a mismatch of energy levels of the two potential wells, thus reducing the probability of quantum mechanical tunneling [50]. The longest relaxation times experimentally determined are of order years under applied magnetic fields $\sim 1$ T, see e.g. [51]. However, for e.g. the same SMM in [51], the low temperature, zero field relaxation time is $\sim 10$ s. Assuming that the time taken to ramp up the magnetic field is $\sim 10^{-5}$ s, then, even if this relaxation time remained at the zero field value (which it will not, because it has a strong dependence on the magnetic field), there is a $\sim 10^{-6}$ probability for a single spin to flip. This is still below what could cause an avalanche, since the probability for a region of radius a few spins long to all flip is still negligible in a crystal with $10^{15} - 10^{18}$ molecular magnets. In reality, we expect that a negligible fraction of spins will flip in the ramp-up, such that the fraction of spins in the meta-stable state remains $\sim 0.5$, with no avalanche occurring during preparation.
B. Threshold tuning

We consider DM depositing heat in the crystal; this could be via a scattering or an absorption mechanism. The heat causes a local increase in temperature, and we exploit the fact that the relaxation times of SMMs are exponentially sensitive to temperature. If this high temperature relaxation time is short compared to the thermal diffusion time scale from that region, then this will cause the spins in that region to relax from their metastable state to the stable state, releasing their stored Zeeman energy.

Consider an energy deposit, \( E_0 \), in a region of size \( R^3 \). The temperature of this region is raised by \( \Delta T \),

\[
\frac{dE}{dT} = C(T) \sim c_0 R^3 T^3 \implies \Delta T = \left( \frac{E_0}{c_0 R^3} \right)^{1/4},
\]

where \( c_0 \) is the volume-specific heat capacity, and where we take a typical temperature dependence for the heat capacity of a crystal at low temperature (this Debye behaviour has been observed in SMMs down to temperatures of 1 K see e.g. [52, 53]). The magnetic relaxation time of the spins in this hot region becomes

\[
\tau \simeq \tau_0 \exp \left( \frac{U - \frac{1}{2} \Delta E_{\text{Zee}}}{{\Delta T}} \right),
\]

where the energy barrier appearing in the Arrhenius law part of eq. (1) has modified by the Zeeman splitting,

\[
\Delta E_{\text{Zee}} = 2 \mu_B g_J J B.
\]

Typical values of \( E_{\text{Zee}} \) range from 0.01 – 0.1 meV.

If the initial hot region is of radius \( R \), the thermal diffusion time scales \( \propto R^2 \), while the spin relaxation time is independent of \( R \). Thus, for a sufficiently large \( R \), the spins will relax before the heat dissipates. So for a given choice of parameters, there is a critical size \( R \) that needs to get heated up for the spins to relax. The energy released from this spin relaxation will then cause other spins to flip, heating up a larger region. The heat from this larger region will take longer to dissipate, and thus all the spins there will also relax, resulting in the deflagration.

The temperature rise \( \Delta T \) caused by this interaction must reduce the magnetic relaxation time \( \tau \lesssim \tau_D \) where the thermal diffusion time \( \tau_D \sim R^2 / \alpha \), \( \alpha \) being the thermal diffusivity. Taking \( \alpha \sim 10^{-7} \text{ m}^2/\text{s} \) at 1K (typical of a number of materials, including water and at least one SMM [54]), we have for \( R \sim 3 \text{ nm}, \tau_D \sim 10^{-10}\text{s} \). In such a material, if an energy
FIG. 5. Tuning curves for a SMM with $U = 50$ K ($\simeq 4.3$ meV), $\tau_0 = 5 \times 10^{-12}$ s, and for $\Delta E_{\text{Ze}} = (0, 0.001, 0.01, 0.1)$ meV (blue solid, green dot-dash, yellow dash, red dot).

deposition within a region of radius 3 nm increases the temperature of that region to cause spin relaxation within $\sim 10^{-10}$ s, the spins can flip and so this energy deposit could trigger a deflagration wave.

Under what conditions does the spin avalanche occur? To address this we turn to aspects of tuning the detector i.e. the balance between the parameters $U$, $J$, $\tau_0$ etc.. The condition for spins to flip in a region of size $R$ is $\tau \lesssim \tau_D$, that is,

$$\tau_0 \exp \left( \frac{U - \frac{1}{2} \Delta E_{\text{Ze}}}{\Delta T} \right) \lesssim \frac{R^2}{\alpha}.$$  \hspace{1cm} (5)

Substituting for $\Delta T$ using eq. (2), this implies that the energy deposit in this region must satisfy

$$E_0 \gtrsim \frac{c_0 R^3 (U - \frac{1}{2} \Delta E_{\text{Ze}})^4}{\ln \left[ \frac{R^2}{\tau_0 \alpha} \right]^4}.$$  \hspace{1cm} (6)

The solid blue curve in Fig. 5 illustrates this inequality for an SMM with parameters $U = 50$ K ($\simeq 4.3$ meV), $\tau_0 = 5 \times 10^{-12}$ s, and $\Delta E_{\text{Ze}} = 0$ (zero field case); we take typical values for the parameters $\alpha = 10^{-7}$ m$^2$/s, and $c_0 = 2 \times 10^{-9}$ eV/K$^4$/nm$^3$. We see the presence of an energy gap $\sim U^4 (\tau_0 \alpha)^{3/2} c_0$; the threshold would be higher/lower if we pick a SMM whose with larger/smaller values of $U$ or $\tau_0$.

We can gain a conservative estimate how much Zeeman energy is needed to fuel an avalanche by asking what $E_0$ would be required to satisfy $\tau \lesssim \tau_D$ if we allow that the Zeeman energy inside the region has already been released and has all converted to heat.
in this region; if we find that progressively less input energy is needed, we find that an avalanche will occur. We set $E_0 \rightarrow E_0 + \rho_s R^3 \Delta E_{Zee}$, where $\rho_s$ is the density of nanomagnets ($\sim 1/\text{nm}^3$). This modifies eq. (6),
\[ E_0 \gtrsim \frac{c_0 R^3 (U - \frac{1}{2} \Delta E_{Zee})^4}{\ln \left[ \frac{R^3}{\tau_0} \right]} - \rho_s R^3 \Delta E_{Zee}, \tag{7} \]
which is plotted as the broken lines in Fig. 5 for different values of $\Delta E_{Zee}$. The Zeeman energy pulls the ‘tuning’ curve over, eventually to negative values of $E_0$, indicating the onset of the avalanche.

Hence, if we take a crystal with $\tau_0 \sim 10^{-11}$ s, with $U \sim 50$ K, we can see that an energy deposit of $\sim 0.01$ eV within $\sim 3$ nm would be sufficient to flip the spins in this region. This will trigger an avalanche in the presence of an external magnetic field $\sim 0.1 - 1$ T, i.e. such that $\Delta E_{Zee} = 0.01 - 0.1$ meV for nanomagnets of spin $J$ in the range $10 - 50$.

There are a number of magnets with parameters in this desired range, though the experimental reports do not in general contain all the necessary data (i.e. such as the actual thermal diffusivity of the material, or zero and non-zero magnetic field relaxation times) necessary to identify a particular material that can be used for dark matter detection.

C. Deflagration quenching

Under the assumption of a large SMM crystal (case a) in II) we now examine in some detail the quenching process. When the external magnetic field is turned off, the Zeeman energy release that drives the deflagration is removed, quenching the process. The speed of the deflagration wave is $\sim 1$ nm/$\tau$ where $\tau \sim \tau_0$ is the actual relaxation time of the spins, with the “burning” occurring layer by layer. This yields a deflagration front moving with a sub-sonic speed $\sim 100$ m/s through the material. It can be seen that with a magnetometer of sensitivity $\sim 0.1$ fT/$\sqrt{\text{Hz}}$ [3], the spin-flips caused by this front would be visible after a period of $\sim 10^{-7}$ s, once it burns through $\sim 10$ $\mu$m of the material. After this time, if the magnetic field is shut off, the flame front will turn off, protecting the remainder of the material.

When switching off the magnetic field, the energy stored in it needs to be removed. If the device is operated with a magnetic field $\sim 0.1$ T and a volume of $\sim (10 \text{ cm})^3$ (corresponding to a $\sim$ kg scale target mass), the energy stored in the field is $\sim 10$ J that can be dissipated in a suitable resistor in $10^{-7}$ s.
D. Reset

We note that the turnoff of the magnetic field is a mechanism which naturally resets the detector. This may occur periodically to quench deflagrations in relatively large crystals, or may become periodically necessary when a certain number of grains have changed state and have become inactive.

V. ABSORPTION OF A DARK VECTOR

To illustrate the potential capability of such a detector, we consider the direct absorption of a dark vector particle. We estimate the sensitivity for absorption of a dark vector in the meV–eV mass range, where the hidden photon mass equals that of a vibrational resonance of the molecules in the crystal, or a low-energy electronic transition in the molecule. We are specifically targeting energies below that of ionization, where we expect existing technologies to be competitive.

The Lagrangian for a dark vector with Stuckelberg mass $m_V$ is

$$\mathcal{L} = -\frac{1}{4} F_{\mu\nu}^2 - \frac{1}{4} V_{\mu\nu}^2 - \frac{\kappa}{2} F_{\mu\nu} V^{\mu\nu} + \frac{m_V^2}{2} V_\mu V^\mu + e J_{em}^\mu A_\mu ,$$

(8)

where $F_{\mu\nu}$ and $V_{\mu\nu}$ are field strength tensors for the photon, $A_\mu$ and dark vector $V_\mu$ fields, $\kappa$ is the kinetic mixing angle, and $J_{em}^\mu$ is the electromagnetic current.

The DM absorption rate is

$$R = \frac{1}{\rho} \frac{\rho_{DM}}{\rho m_{DM}} \langle n \sigma_{abs} v \rangle ,$$

(9)

where $\rho$ is the density of the crystal, $\rho_{DM} \sim 0.3 \text{GeV/cm}^3$ is the local DM mass density, $m_{DM} = m_V$ for the dark photon model of eq. $[8]$, $n$ is the number density of the molecules in the crystal, $\sigma_{abs} = \sigma_{abs}(m_V)$ is the DM–molecule absorption cross section, and the local DM velocity $v \sim 10^{-3}$. We follow Refs. $[55, 56]$ in relating the dark vector absorption cross section to that of photons, taking into account in-medium effects,

$$\langle n \sigma_{abs}(m_V) v \rangle = \kappa_{eff}^2 \langle n \sigma_{abs}^\gamma(\omega = m_V) c \rangle ,$$

(10)

where $\sigma_{abs}^\gamma(\omega = m_V)$ is the EM photon–molecule absorption cross section for photons of energy $\omega$, and where for clarity we restored a factor of $c$. The effective in-medium mixing angle is defined as,

$$\kappa_{eff}^2 \simeq \kappa^2 \frac{1}{|\epsilon(\omega)|^2} ,$$

(11)
where $\epsilon$ is the relative permittivity of the SMM. In the below we put bounds on this effective mixing angle. The bounds on $\kappa$ would follow through eq. (11) using data on the relative permittivity of an SMM in a more detailed study; because SMMs are insulators, we expect that this is a small effect (i.e. the sensitivity to $\kappa$ is within one or two orders of magnitude of that of $\kappa_{\text{eff}}$ across the entire energy range we consider—we explicitly verified this in our representative example below in regions of energy where such data was available.).

There is currently little available detailed data on the IR absorption spectrum of the majority of known SMM crystals. To obtain a representative example of the sensitivity to the dark vector model we use data taken on the first discovered and most widely studied SMM, Mn$_{12}$O$_{12}$-acetate (Mn$_{12}$-acetate). Although this SMM does not have the desired tuning parameters to be used as a DM detector, the absorption of EM radiation of energy $\gtrsim$ meV that we consider is not sensitive to such parameters that are properties of the entire molecule. (Absorption of light of frequency Hz-MHz is dependent on such properties, see e.g. Ref. [57].)

In the meV–100 meV regime, photons are absorbed by the vibrational modes between ions in the molecule (e.g. Mn-O, C=O, etc.)—while these give rise to spectral ‘fingerprints’ that differ depending on the composition of the SMM, the broad features are similar. For instance any molecule with a C=O bond will show an absorption feature in the 190–220 meV region. Similarly, the Mn-O bond is of course absent in SMMs based on different metallic ions, but will be replaced by e.g. a Fe-O, Fe-N, Dy-O etc. bond that absorbs at a different frequency.

In the 100 meV–10 eV regime, EM absorption takes place via a restructuring of electronic configurations in the molecule. The spectrum for this compound has been found to be anomalously diffuse [58] (in line with theoretical predictions [59, 60]), with very broad excitations identified e.g. Mn inner $\rightarrow$ outer and O p $\rightarrow$ Mn d charge transfers.

For the meV–100 meV regime we use data from Ref. [61], and for 100 meV–10 eV we use data from Ref. [58]; from this we are able to obtain $\sigma_{\text{abs}}$ for Mn$_{12}$-acetate. See App. A for further details.

The above absorption mechanisms that we are exploiting are localised—they are intra-molecular excitations. This is very different to excitations of phonon modes that are coherent across the entire crystal; such modes require long-range order. In principle, inter-molecular excitations would lead to such phonon modes (at lower energies); however, crystal defects and impurities change the phonon spectrum significantly. In general, we expect that such
FIG. 6. Estimated sensitivity to absorption of dark vector DM in Mn$_{12}$-acetate, assuming an aggressive sensitivity of 1 event/kg year. The absorption data from Refs. [58], [61] (described in the appendix) has been smoothed, and an interpolation used in the region $m_V \sim 0.2 - 0.5$ eV, for which no data was available.

Disorder could be advantageous, as localisation typically leads to larger absorption (or scattering) cross sections through making many more phonon modes available for radiation to couple to (also, these phonon modes typically give zero-order EM dipoles). Describing such processes theoretically, however, is more difficult than in a very pure system, and we postpone a detailed discussion to future work; for the present we use the available data for the localised absorption processes that are active at the energies considered above.

Using the absorption data for Mn$_{12}$-acetate, we plot the expected sensitivity to the dark vector model in Fig. 6, assuming an aggressive sensitivity of 1 event per kg-year. The neutrino background in the 1 – 100 meV range of energy is approximately 1 / kg-year [62], and as such the curves rest upon the neutrino floor; above this energy the curve is above the floor. Also shown are existing exclusion limits on the model of eq. (8), from stellar [55] and the Xenon10 experiment [56]. The only limits that exist in the region where we plot SMM projections are set by stellar bounds. Our results suggest that an improvement in sensitivity over the entire energy range is possible, with an improvement of several orders of magnitude in the meV–10 meV region. This would significantly extend the reach of DM
direct detection experiments below the current lower bound on mass.

VI. CONCLUSIONS

We have discussed the potential of single molecule magnets for use in the direct detection of DM, with energy thresholds down to $\sim$ meV. These crystals possess a built-in amplification mechanism—magnetic deflagration, or a spin avalanche—a phenomenon that is tunable, such that a detector concept that operates in a similar fashion to a conventional bubble chamber can be envisaged.

The mechanism that sets off the spin deflagration is rather general—any process that deposits enough localised heat in the crystal will trigger it. The energy gap, or threshold, for this is one of the tunable aspects of our concept. Residual radioactive backgrounds need to be studied, but there is hope that they can be managed to an acceptable level. We mention here that a prototype experiment running with a higher threshold of $\sim$10 eV per $\sim$nm$^3$ region would not be triggered by electron backgrounds, since the energy loss of an electron as it passes through the detector falls below this threshold (see e.g. [63]).

Importantly, the spin deflagration mechanism does not require a pure sample—impurities and defects (disorder) do not need to be eliminated. This touches on a perhaps more important general observation: disorder can be tolerable, and even advantageous, since it typically causes localisation that brings about larger interaction cross sections.

The outcome of the current work suggests it would be good to study more general glassy materials, e.g. spin glasses, to determine which possess the most favourable DM detector qualities. For instance, in the SMM crystals that we have surveyed, we need temperatures of $\sim$0.1 K in order to make the meta-stable state ‘stable’ on a detector run timescale. It is possible that other frustrated systems could realize these conditions at higher temperatures, which could significantly improve the experimental condition.

We used readily available IR absorption data to estimate the projected sensitivity to a dark vector model of DM. We found a sensitivity extending three orders of magnitude in mass below that of existing experiments, and several orders of magnitude below that of existing astrophysical bounds. To fully explore the sub-GeV DM parameter space, including scalar and fermionic DM, other triggering mechanisms should be investigated (e.g. Raman scattering, scattering in general).

Given the relatively low cost and ease of growing SMM crystals, and the prospects demon-
strated in this study, we believe there is a strong case to begin to experimentally examine their use as DM detectors.

ACKNOWLEDGMENTS

We would like to thank the Heising-Simons Foundation for organizing a workshop at UC Berkeley during which this idea was conceived, and Simon Knapen, Steve Liddle, Tongyan Lin, Dan McKinsey and Matt Pyle for useful discussions. PB is supported by U.S. NSF grant CHE-1464841; GG is supported, in part, by U.S. DOE grant DE-SC0009841; TM is supported by U.S. DOE grant DE-AC02-05CH11231, and by WPI, MEXT, Japan; SR was supported in part by the NSF under grants PHY-1417295 and PHY-1507160, the Simons Foundation Award 378243 and the Heising-Simons Foundation grant 2015-038.

Appendix A: Absorption in Mn$_{12}$-acetate

In Fig. 7 we reproduce the transmittance, $T$, for Mn$_{12}$-acetate which was presented in Ref. [61], in the frequency ranges $30 - 70$ cm$^{-1}$ and $140 - 650$ cm$^{-1}$. This data is taken at zero magnetic field and at 10 K. In this experiment Mn$_{12}$-acetate was finely ground and distributed in a paraffin pellet, of thickness $l$, at a concentration $h$ ($h = 0.85$ and $h =$
0.035 for the two different curves shown in Fig. 7. The spectral lines in this frequency range are largely identified with Mn-O bond vibrations. While pronounced trough positions are reasonably stable under temperature (the range 10 K-100 K was studied), they sharpen slightly at lower temperatures. In an external magnetic field, as would be the case in the running of our proposed DM detector, these troughs broaden and shift to a small degree.

If reflection is neglected, the absorption coefficient, $\alpha(\omega)$, can be obtained from the transmittance via the Beer-Lambert law,

$$T(\omega) = \exp(-\alpha(\omega) l h).$$  \hspace{1cm} \text{(A1)}

Reflection measurements were not reported in [61], and in fact the authors of that work calculate relative absorption using eq. (A1). Thus we infer that the reflectance in the experimental setup was small (this is plausible given the SMM was finely ground and distributed in paraffin), such that eq. (A1) is a good approximation. The thickness, $l$, was also not reported; we fix this parameter by matching onto the calculated absorption spectrum at higher energies, presented below.

Ref. [58] studies both transmittance and reflectance of Mn$_{12}$-acetate crystals over the frequency range 600-50,000 cm$^{-1}$. From this the authors calculate the absorption spectrum for light incident both parallel and perpendicular to the magnetic anisotropy axis; we reproduce the average in Fig. 8. In the low energy data sample, spectral peaks at 600 cm$^{-1}$ are again observed and correspond to vibrations of the Mn$_{12}$ crown; spectral features around

![Absorption spectrum for Mn$_{12}$-acetate, reproduced from Ref. [58].]
\[ \sim 1000 - 1500 \text{ cm}^{-1} \] are identified in Ref. \[64\] as Mn-acetate, C-O, and acetate stretching in Raman scattering data (in \[64\], similar ‘ligand’ resonances in IR absorption of the SMM \[Fe_8Br_8\] \[65\] were also identified). Several higher energy, very broad spectral features are identified in \[58\], \emph{e.g.} a density of states effect related to a charge transfer between Mn ions at \[15900 \text{ cm}^{-1} \], and a charge transfer from O to Mn ions \[36600 \text{ and } 42350 \text{ cm}^{-1} \]—these are not easily seen in Fig. \[8\].

The EM absorption cross section is directly related to the absorption coefficient,

\[
\sigma_{\text{abs}}(\omega) = \alpha(\omega) n , \tag{A2}
\]

where \(n\) is the number density of molecules.

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